$$\begin{split} f &= \frac{A - B}{A + B}, \\ f &= \frac{A}{(A + B)} - \frac{B}{A + B} \\ \delta f &= \sqrt{\left(\frac{\partial f}{\partial A}\delta A\right)^2 + \left(\frac{\partial f}{\partial B}\delta B\right)^2} \\ &\frac{\partial f}{\partial A} = \frac{1(A + B) - A}{(A + B)^2} - \frac{-B}{(A + B)^2} = \frac{2B}{(A + B)^2} \\ &\frac{\partial f}{\partial B} = \frac{-A}{(A + B)^2} - \frac{1(A + B)B}{(A + B)^2} = \frac{-2A}{(A + B)^2} \\ &\delta f = \sqrt{\left(\frac{2B}{(A + B)^2}\delta A\right)^2 + \left(-\frac{2A}{(A + B)^2}\delta B\right)^2} \\ &\delta f = \frac{2}{(A + B)^2}\sqrt{B^2\delta A^2 + A^2\delta B^2} \end{split}$$

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Equation S1. Finding the formula for error propagation through the normalization formula used to calculate pairwise comparisons depicted in Figure 2 and Figure S2. The formula compares taxonomic classes relative enrichment between two experimental conditions as well as scaling. The classes are expressed as A and B and the standard error corresponds to δA and δB respectively. The resulting normalized standard deviation is represented as δf .