

Towards Efficient Verifiable Multi-Keyword Search over Encrypted Data based on Blockchain

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Abstract

Searchable symmetric encryption (SSE) provides an effective way to search encrypted data stored on untrusted servers. As we all known, the server is not trusted, so it is indispensable to verify the results returned by it. However, the existing SSE schemes either lack fairness in the verification of search results, or do not support the verification of multiple keywords. To address this, we design a multi-keyword verifiable searchable symmetric encryption scheme based on blockchain, which provides an efficient multi-keyword search and fair verification of search results. We utilize bitmap to build search index in order to improve search efficiency, and use blockchain to ensure fair verification of search results. The bitmap and hash function are combined to realize lightweight multi-keyword search result verification, compared with the existing verification schemes using public key cryptography primitives, our scheme reduces the verification time and improves the verification efficiency. In addition, our scheme supports the dynamic update of files and realizes the forward security in update. Finally, formal security analysis proves that our scheme is secure against Chosen-Keyword Attacks (CKA), experimental analysis demonstrates that our scheme is efficient and viable in practice.

Introduction

With the development of artificial intelligence, Internet of things, Internet of vehicles and other emerging technologies, more and more enterprises and individuals outsource local data to the cloud, thereby reducing storage and management overhead. However, security and privacy concerns still hinder the deployment of cloud storage system. Although data encryption can eradicate such concerns to some extent, it becomes difficult for users to search over the data.

40 Searchable symmetric encryption (SSE) provides an efficient mechanism to solve this, which
41 enables users to search encrypted data efficiently without decryption. Since SSE was first proposed
42 by Song (Song, Wagner & Perrig, 2000), how to perform efficient and versatile search on
43 encrypted data has always been an important research direction. The existing SSE schemes mainly
44 use linked lists and vectors to build indexes, the cloud server needs to traverse the whole list or
45 vector to search for matching results during a query, which incurs high search overhead. In addition
46 to efficient search, dynamic updates are also very important in SSE. (Zhang, Katz & Papamanthou, 2016)
47 has shown that adversaries can infer the critical information through the file injection attacks
48 during the dynamic update of the SSE, while the forward-secure SSE can avoid this. Therefore,
49 the forward security of the scheme must be fully considered when designing the SSE scheme.

50 Verifiability of the search results is another important research issue for SSE. Since The cloud
51 server is untrusted, which may returns incorrect or incomplete results due to system failures or
52 cost savings, so, it is necessary to verify the search results. In 2012, (Qi & Gong, 2012) proposed
53 the concept of verifiable SSE (VSSE) and constructed a verifiable SSE scheme based on word tree.
54 Following this work, a great many VSSE schemes are proposed (Kurosawa & Ohtaki, 2012; Zhu, Liu
55 & Wang, 2016; Liu et.al 2017; Zhang et.al 2019;Chen et.al 2021). In these schemes, the verification is
56 mainly performed by users, but the user may forge verification results to save costs, so the
57 reliability of the verification cannot be guaranteed. To address this, some researchers(Hu et.al 2018;
58 Li et.al 2019; Guo, Zhang & Jia , 2020) introduce blockchain into SSE to verify search results,
59 which guarantees the fairness and reliability of the verification. Although blockchain achieves fair
60 verification of search results, but the existing schemes are only for a single keyword, and there is
61 little research on fair verification for multi-keywords.

62 In this paper, we introduce a verifiable multi-keyword SSE scheme based on blockchain, which
63 can perform efficient multi-keyword search, ensures the fairness of verification, and supports the
64 dynamic update of files. To our knowledge, this is the first scheme to verify the search results of
65 multi-keywords fairly. In general, the contributions of this paper are summarized as follows:

- 66 • Our scheme realizes efficient multi-keyword search and verification of search results, at the
67 same time, our scheme supports dynamic update of files and achieves forward security.
- 68 • Our scheme utilizes blockchain to verify the search results, ensuring the reliability and fairness
69 of the verification results. Combining bitmap index and hash function, we realize lightweight
70 multi-keyword verification to improve verification efficiency.
- 71 • We formally prove that our scheme is adaptively secure against CKA, and we conduct a series
72 of experiments to evaluate the performance of our scheme.

73

74 **Related Works**

75 **Searchable Symmetric Encryption**

76 Since SSE was proposed, a number of works have been done to improve search efficiency, rich
77 expression and advanced security. The first SSE scheme (Song, Wagner & Perrig, 2000) enables
78 users to search keywords through full-text scanning, search time increases linearly with the size of
79 files, which is impractical and inefficient. To improve efficient, Curtmola et.al (2006) proposed an

80 inverted index SSE, which achieves sub-linear search time, and gives a definition of SSE security,
81 but this scheme does not support dynamic operations. Wang, Cao & Ren (2010) expanded the
82 scheme of Curtmola et.al (2006) to support dynamic operations, and proved that the scheme was
83 adaptively secure against chosen-keyword attacks (CKA2-secure). For the schemes that support
84 dynamic operation, forward security is critically crucial. The research of Cash et.al (2013) and
85 Zhang, Katz & Papamanthou (2016) indicated that in the SSE scheme without forward security, the
86 adversary can recover most of the sensitive information in ciphertext at a small cost, their research
87 shows the importance of forward security.

88 Multi-keyword search is a crucial means to improve search efficiency. In single-keyword search
89 scheme (Song, Wagner & Perrig,2000; Curtmola et.al, 2006; Wang, Cao & Ren, 2010), the server returns
90 some irrelevant results, while the multi-keyword search (Cash et.al, 2013; Lai et.al, 2018; Xu et.al,
91 2019;Liang et.al 2020;Liang et.al 2021) gains higher search accuracy and more accurate results.
92 To further improve search efficiency, Abdelraheem et.al (2016) proposed an SSE scheme on
93 encrypted bitmap indexes to support multi-keyword search, but requires two rounds of interactions
94 with the cloud server. Zuo et.al (2019) proposed a secure SSE scheme based on bitmap index
95 which supports dynamic operations with forward and backward security, but this scheme lacks the
96 verification of the results.

97

98 **Verifiable Searchable Symmetric Encryption**

99 In SSE, it is necessary to verify the results since the server is untrusted. Qi & Gong (2012) proposed
100 the concept of verifiable searchable symmetric encryption (VSSE) and constructed a VSSE
101 scheme based on word tree. Along this direction, some other VSSE schemes (Kurosawa & Ohtaki,
102 2012; Zhu, Liu & Wang ,2016; Liu et.al ,2017,Miao et.al 2021) are proposed. These schemes are
103 the verification of single keyword search results, Azraoui et.al (2015) combined polynomial-based
104 accumulators and Merkle trees to achieve conjunctive keyword verification. Wan & Deng (2018)
105 used homomorphic MAC to verify the results of multi-keyword search. Li et.al (2021) utilized
106 bitmap index to gain high efficiency of multi-keyword search, and verified the results by RSA
107 accumulator. Ge et.al (2021) and Liu et.al (2021) proposed their verifiable schemes in the Internet
108 of things. These schemes verify the results of multi-keyword search by public key cryptography
109 primitives, which is computationally expensive and inefficient. What is more, these multi-keyword
110 search verifiable schemes mainly focus on verifying the returned files are valid and whether the
111 files really contains the query keywords, but they didn't ensure all files containing the query
112 keywords are returned.

113

114 **Verifiable Searchable Symmetric Encryption Based on Blockchain**

115 In the existing SSE schemes, the verification of search results is performed by users. However,
116 users may forge verification results for economic benefits, which damages the fairness of
117 verification. To solve this, a flexible and feasible method is to adopt blockchain to verify search
118 results, which uses the non-repudiable property of the blockchain to ensure the reliability and
119 fairness of verification. Hu et.al (2018) built a distributed, verifiable and fair ciphertext retrieval

120 scheme based on blockchain. Li et.al (2019) proposed a verifiable scheme combined blockchain
121 and SSE, which can verify the results automatically and reduce the calculation of users. Guo,
122 Zhang & Jia (2020) used the blockchain to realize the public authentication of search results, and
123 ensures forward security of dynamic update. Although these schemes realize the fair verification
124 of search results, but they are mainly for single keyword search, whereas there is little research on
125 the fair verification of multi-keyword. Comparison results with existing schemes are shown in
126 Table 1.

127

128 Preliminaries

129 Bitmap

130 To improve search efficiency, we use the bitmap (Spiegler & Maayan, 1985) to build inverted index.
131 Bitmap uses a binary string to store a set of information, which can effectively save storage space,
132 and it has been widely used in the field of ciphertext retrieval. In our scheme, each keyword w_i
133 corresponds to a bitmap, which contains ℓ bits, ℓ is the number of files in the system, if the i -th
134 document contains w_i the value of ℓ in position i is 1, otherwise 0. For example, there are four
135 files (f_1, f_2, f_3, f_4) and two keywords (w_1, w_2) , in Fig.1, w_1 is contained in f_1 and f_3 , w_2 is
136 contained in f_2 and f_3 , the bitmap of w_1 and w_2 are 1010 and 0110. If we want to search files
137 that contains both w_1 and w_2 , we need to do AND operation on the two bitmaps, i.e.
138 $1010 \wedge 0110 = 0010$, that indicates that f_3 contains both w_1 and w_2 .

139

140 Blockchain

141 Blockchain is a distributed database, which is widely used in emerging cryptocurrencies to store
142 transaction information such as bitcoin. The blockchain has the features of decentralization,
143 transparency and unforgeability. There is no central server in the blockchain, all nodes participate
144 in the operation and generate the calculation results, the information stored on the blockchain can
145 be seen by all nodes in the network. All nodes of the blockchain share the same data record, under
146 the action of the consensus mechanism, a single node cannot modify the data stored on the chain.
147 The above characteristics of blockchain make it suitable to be a trusted third party for fair
148 verification.

149

150 Method

151 System Model

152 The system model of our scheme is shown in Fig.2, there are four entities in the system: data owner,
153 cloud server, data user, blockchain. For the files \mathbf{F} in the system, data owner extracts all keywords
154 and generates a keyword set \mathbf{W} . Data owner encrypts files to a database T , builds an encrypted
155 index T_B and a checklist B , T_B and T are sent to cloud server, T_B and B are sent to blockchain.
156 When a data user joins the system, it sends an authentication request to the data owner, obtains

157 keys and system parameters. During a query, the data user generates search token $TK_{i,Q}$ according
 158 to the keywords to be queried with the help of keys and system parameters, and then sends it to
 159 cloud server and blockchain, respectively. Cloud server provides storage services for index T_B
 160 and T . In addition, the cloud server performs ciphertext retrieval according to the search token
 161 $TK_{i,Q}$, and sends the matched results to blockchain for verification.

162 To verify the search results of multiple keywords, the blockchain performs two steps: 1)
 163 benchmark. On receiving $TK_{i,Q}$, the blockchain performs multi-keyword search on the index T_B
 164 to get the identifiers ID of files that meets the query, then gets the corresponding hash values \mathbb{H}
 165 of files from the checklist B according ID , and computes the benchmark Acc using \mathbb{H} ; 2)
 166 verification. After receiving the results returned by cloud server, the blockchain computes the hash
 167 values \mathbb{H}' of results and computes the verification value Acc' , then the blockchain compares
 168 Acc and Acc' to generate the proof. The proof and search results are sent to data user, the
 169 verification is completed.

170

171 Threat Model

172 Like other verifiable SSE schemes (Soleimanian & Khazaei, 2019), we assume that the cloud server
 173 is malicious, which may return an incorrect or incomplete search result for selfish reasons, such as
 174 saving bandwidth or storage space. In addition, we assume that the data user is also untrusted,
 175 since it may forge the verification results for economic benefits. The data owner and blockchain
 176 are trusted, they execute the protocols in the system honestly.

177

178 Algorithm Definitions

179 Our scheme includes eight polynomial time algorithms, $\Pi = \{\text{Keygen}, \text{Setup}, \text{ClientAuth}$
 180 $\text{TokenGen}, \text{Search}, \text{Verify}, \text{UpdateToken}, \text{Update}\}$, and the details are as follows:

- 181 • $K \leftarrow \text{KeyGen}(1^\lambda)$, takes system parameter λ as input, and outputs system keys K .
- 182 • $(T, T_B, B) \leftarrow \text{Setup}(K, \mathbf{W}, \mathbf{F})$, takes system keys K , the keyword set \mathbf{W} and the set of files
 183 \mathbf{F} as input, outputs a database of encrypted files T , an encrypted index T_B and a checklist B .
- 184 • $(K_1, \Sigma) \leftarrow \text{ClientAuth}(\mathbb{A}_i)$, takes the attribute \mathbb{A}_i of user as input, outputs secret key K_1 and
 185 the keyword status Σ .
- 186 • $TK_{i,Q} \leftarrow \text{TokenGen}(K_1, \overline{\mathbf{W}})$, takes secret key K_1 , a set of keywords to query $\overline{\mathbf{W}} = \{w_1, w_2, \dots,$
 187 $w_t\}$, outputs the search token $TK_{i,Q}$.
- 188 • $(R, Acc) \leftarrow \text{Search}(T, T_B, B, TK_{i,Q})$, takes search token $TK_{i,Q}$, the encrypted database T ,
 189 encrypted index T_B and the checklist B as input, and outputs the search results R and the
 190 benchmark Acc .

- 191 • $(R, proof) \leftarrow \text{Verify}(R, Acc)$, takes the search results R , and the benchmark Acc as input,
- 192 outputs the verification proof $proof$ and results R .
- 193 • $(\tau_s, \tau_b) \leftarrow \text{UpdateToken}(\bar{\mathbf{F}}, \mathbf{W}', K)$, takes the set of files to update $\bar{\mathbf{F}}$, the set of keywords \mathbf{W}'
- 194 and system keys $K = \{K_1, K_2, K_3\}$ as input, and outputs the update token (τ_s, τ_b) .
- 195 • $(\mathbf{T}', \mathbf{T}_B', \mathbf{B}') \leftarrow \text{Update}(\mathbf{T}, \mathbf{T}_B, \mathbf{B}, \tau_s, \tau_b)$, takes encrypted database \mathbf{T} , encrypted index \mathbf{T}_B and
- 196 the update token (τ_s, τ_b) as input, outputs the updated database \mathbf{T}' , updated index \mathbf{T}_B' and the
- 197 updated checklist \mathbf{B}' .

198

199 Security Definitions

200 We prove the security of our scheme with the random oracle model, which can be executed by two
 201 probabilistic games $\text{Real}_{\mathcal{A}}(\lambda)$ and $\text{Ideal}_{\mathcal{A}, \mathcal{S}}(\lambda)$, and we have the following definitions:

202 **Definition 1** : CKA2-security, for the verifiable multi-keyword search scheme
 203 $\Pi = \{\text{KeyGen}, \text{Setup}, \text{ClientAuth}, \text{TokenGen}, \text{Search}, \text{Verify}, \text{Update}\}$, let $\mathcal{L} = \{\mathcal{L}_{\text{setup}}, \mathcal{L}_{\text{search}}, \mathcal{L}_{\text{update}}\}$ be
 204 the leakage function, \mathcal{A} is the adversary and \mathcal{S} is the simulator, there are two probabilistic
 205 experiments:

206 $\text{Real}_{\mathcal{A}}(\lambda)$: The challenger runs $\text{KeyGen}(1^\lambda)$ to generate secret key $K = \{K_1, K_2, K_3\}$, the
 207 adversary \mathcal{A} outputs \mathbf{F} and \mathbf{W} . The challenger triggers this experiment to run $\text{Setup}(K, \mathbf{W}, \mathbf{F})$,
 208 outputs the index \mathbf{T}_B, \mathbf{T} and \mathbf{B} , which are sent to \mathcal{A} . \mathcal{A} generates a series of adaptive queries
 209 $Q = \{q_1, q_2, \dots, q_t\}$, for each $q_i \in Q$, the challenger generates search or update tokens, \mathcal{A} receives
 210 those tokens and generates a bit b as the output of this experiment.

211 $\text{Ideal}_{\mathcal{A}, \mathcal{S}}(\lambda)$: The adversary \mathcal{A} outputs \mathbf{F} and \mathbf{W} , the simulator \mathcal{S} generates the index \mathbf{T}_B, \mathbf{T}
 212 and \mathbf{B} through $\mathcal{L}_{\text{Setup}}$, \mathcal{A} receives them. \mathcal{A} generates a series of adaptive queries
 213 $Q = \{q_1, q_2, \dots, q_t\}$, for each $q_i \in Q$, the simulator \mathcal{S} generates search or update tokens with $\mathcal{L}_{\text{Search}}$
 214 and $\mathcal{L}_{\text{Update}}$, \mathcal{A} receives those tokens and generates a bit b as the output of this experiment.

215 If for any probabilistic polynomial time (PPT) adversary \mathcal{A} , there exist an efficient simulator
 216 \mathcal{S} , which satisfies that:

$$217 |\Pr[\text{Real}_{\mathcal{A}}(\lambda) = 1] - \Pr[\text{Ideal}_{\mathcal{A}, \mathcal{S}}(\lambda) = 1]| \leq \text{negl}(\lambda)$$

218 , we say Π is \mathcal{L} -secure against CKA2, where negl is a negligible function and λ is the
 219 security parameter.

220

221 Construction

222 In this section, we present the construction of our scheme in detail. We take bitmap as index
 223 structure to achieve efficient search over encrypted data, and use blockchain to verify the search

224 results. The bitmap is utilized to build the inverted index to achieve the optimal search time
 225 $\mathcal{O}(|q|)$, where q is the keywords in search and $|q|$ is the number of q .

226 In our scheme, the blockchain is used to fairly verify the search results. In Setup, the data owner
 227 calculates the hash value of files, generates a checklist B and saves it on the blockchain. During
 228 the verification, the blockchain smart contract computes the hash values of search results returned
 229 by the server and compares them with the existing results to obtain the verification results.

230 Specifically, in the single keyword setting, the blockchain stores the corresponding benchmark
 231 directly since the results corresponding to the keywords are determined. However, it's impossible
 232 in multi-keyword search because the search results are variable, which can only store the
 233 verification value of each file. To ensure the credibility of the search results, the blockchain also
 234 needs to perform multi-keyword search to obtain the search results. Therefore, we save the index
 235 T_B on the blockchain. During a query, the blockchain executes multi-keyword search to get the
 236 search results, and read the verification value $hash_i$ of each file in search results to generate the
 237 benchmark Acc , then the blockchain compares Acc with search results returned by cloud server
 238 to complete the verification.

239

240 Proposed Construction

241 Our scheme contains eight algorithms $\Pi = \{\text{KeyGen}, \text{Setup}, \text{ClientAuth}, \text{TokenGen}, \text{Search}, \text{Verify}$
 242 $\text{UpdateToken}, \text{Update}\}$, let $F: \{0,1\}^* \rightarrow \{0,1\}^m$, $H: \{0,1\}^* \rightarrow \{0,1\}^n$ be two Pseudo-Random
 243 Functions (PRFs), the constructions of our scheme are as follows.

244 $K \leftarrow \text{KeyGen}(1^\lambda)$: This algorithm is executed by the data owner, given a security parameter
 245 $\lambda \in \mathbb{N}$, this algorithm generates the secret key $K = \{K_1, K_2, K_3\}$, where $K_1, K_2, K_3 \xleftarrow{\$} \{0,1\}^\lambda$, K_1, K_2
 246 are used to encrypt the bitmap index for each keyword $w_i \in \mathbf{W}$, K_3 is used to encrypt files $f_i \in \mathbf{F}$
 247 and store the hash value of files.

248 $(T, T_B, B) \leftarrow \text{Setup}(K, \mathbf{W}, \mathbf{F})$: Given a set of files \mathbf{F} , a set of keywords \mathbf{W} and the secret keys
 249 K , this algorithm builds an encrypted index T_B , a checklist B and a ciphertext database T , as is
 250 shown in Algorithm 1. For each file $f_i \in \mathbf{F}$, id_i is the identifier of f_i , the data owner encrypts f_i by
 251 calculating $c_i \leftarrow \text{Enc}(K_3, f_i)$, and computes the hash value using $hash_i \leftarrow H(c_i)$. Then data owner
 252 stores c_i and $hash_i$ in $T[l_i]$ and $B[l_i]$, respectively.

253 For each keyword $w_i \in \mathbf{W}$, data owner generates a bitmap \mathcal{B}_{w_i} , if id_j contains keyword w_i ,
 254 then $\mathcal{B}_{w_i}[m] = 1$, where $m = H(id_j \| K_3)$, and the other positions of \mathcal{B}_{w_i} are all 0's. The data owner
 255 encrypts \mathcal{B}_{w_i} through $v_B \leftarrow \mathcal{B}_{w_i} \oplus H(t_w \| st_{i+1})$, and store v_B in $T_B[t_w]$. At the end of the Setup,
 256 (T_B, B) and (T, T_B) are sent and stored on blockchain and cloud server, respectively.

257 $(K_1, \Sigma) \leftarrow \mathbf{ClientAuth}(\mathbb{A}_i)$: It needs to register to the data owner when a new data user who
 258 wants to query files on the cloud server joins the system. The data user submits attribute \mathbb{A}_i to the
 259 data owner through this algorithm to obtain the keyword status Σ and the key K_1 .

260 $TK_{i,Q} \leftarrow \mathbf{TokenGen}(K_1, \overline{W})$: It takes the key K_1 and the set of keywords to query
 261 $\overline{W} = \{w_1, w_2, \dots, w_t\}$ as input, output a search token $TK_{i,Q}$, as is shown in Algorithm2. For each
 262 keyword $w_i \in \overline{W}$, the data user computes the position l_{w_i} of w_i in index T_B as $l_{w_i} \leftarrow H(u_{w_i} \parallel st_i)$,
 263 where $u_{w_i} \leftarrow F(K_1, H_1(w_i))$, $st_i \leftarrow \Sigma[w_i]$. Data user sends $TK_{i,Q}$ to cloud server and blockchain,
 264 respectively.

265 $(R, Acc) \leftarrow \mathbf{Search}(T, T_B, B, TK_{i,Q})$: This algorithm takes search token $TK_{i,Q}$, index T_B and
 266 ciphertext database T as input, and outputs search results R . On receiving the search token, the
 267 cloud server and blockchain perform the same operations for multi-keyword search. They all parse
 268 out the position l_{w_i} of the keyword in the token $TK_{i,Q}$, and get the bitmap \mathcal{B}_{w_i} through
 269 $\mathcal{B}_{w_i} \leftarrow v_B \oplus H(K_{w_i} \parallel l_i)$, $v_B \leftarrow T_B[l_{w_i}]$. To achieve multi-keyword search, they compute
 270 $\mathcal{B} = \mathcal{B}_1 \wedge \mathcal{B}_2 \wedge \dots \wedge \mathcal{B}_t$, the cloud server gets files in T according to \mathcal{B} with regard to $\mathcal{B}[i]=1$, and
 271 sends them to the blockchain to verify. Similarly, the blockchain gets hash values
 272 $\{hash_1, hash_2, \dots, hash_s\}$ of files in B according to \mathcal{B} , computes $Acc = hash_1 \oplus hash_2 \oplus \dots \oplus hash_s$
 273 as the benchmark for verification, and the details are shown in Algorithm 2.

274 $(R, proof) \leftarrow \mathbf{Verify}(R, Acc)$: This algorithm takes search results R and benchmark Acc as
 275 input, outputs search results R and $proof$, and the verify process is shown in Algorithm 3. To
 276 verify the integrity of files, the data owner calculates the hash value of each file through
 277 $hash_i \leftarrow H(c_i)$ in the Setup, and adds $hash_i$ to the checklist B , then B is sent to the blockchain.
 278 Through algorithm **Search**, the blockchain gets the search result of multiple keywords, obtains the
 279 hash value of each file in the result from B , and computes the benchmark Acc . To verify the search
 280 results, the blockchain calculates $H_{\overline{W}}$ of R and compares it with Acc .

281 In Algorithm 3, for all ciphertexts $c_i \in R$, blockchain computes $H_{\overline{W}} \leftarrow H_{\overline{W}} \oplus H(c_i)$, where
 282 $H(c_i)$ denotes the hash value of c_i . Blockchain compares $H_{\overline{W}}$ and Acc , if they are equal, the
 283 proof is true, otherwise false. At last, the search results R and proof are sent to data user. During
 284 the verification, Acc is calculated through the hash value stored on the blockchain, due to the
 285 unforgeability of blockchain, thus Acc is unforgeable. In addition, the verification is completed
 286 by the blockchain, so the proof is also unforgeable, which ensures the fairness of verification.
 287

288 $(\tau_s, \tau_b) \leftarrow \mathbf{UpdateToken}(\overline{F}, W', K)$: The data owner generates an update token through this
 289 algorithm, which takes files \overline{F} , a keyword set W' and secret key K as input, and outputs update

290 token (τ_s, τ_b) . For files $f_k \in \bar{F}$, the data owner encrypts and calculates the hash value of f_k by
 291 $c_k \leftarrow \text{Enc}(K_3, f_k)$ and $hash_k \leftarrow H(c_k)$, respectively. For keywords $W' = \{w_1, w_2, \dots, w_s\}$ that
 292 contained in f_k , the data owner generates a bitmap \mathcal{B}_{w_j} for each $w_j \in W'$, and encrypts \mathcal{B}_{w_j} with
 293 $v_B \leftarrow \mathcal{B}_{w_j} \oplus H(l_{w_j} \parallel st)$, where $l_{w_j} \leftarrow H(u_{w_j} \parallel st)$, $u_{w_j} \leftarrow F(K_1, H(w_j))$, $st \leftarrow F(K_2, st_0)$.

294 $(T', T_B', B') \leftarrow \text{Update}(T, T_B, B, \tau_s, \tau_b)$: This algorithm takes encrypted database T , index T_B ,
 295 checklist B , update token (τ_s, τ_b) as input, and outputs updated database T' , updated index T_B'
 296 and updated checklist B' . The details are shown in Algorithm 4.

297

298 **Forward security**

299 As described above, dynamic update is the foundation function of an SSE scheme, and forward
 300 security is an indispensable component of dynamic update. In Algorithm 4, when updating a file
 301 f_i that contains keyword w_j , the data owner retrieves the previous state st_0 from the local state
 302 store Σ , and generates a new state st through $st \leftarrow F(K_2, st_0)$, where F is a pseudo random
 303 function and K_2 is kept in local. To search a keyword w_j , the data user retrieves the current state
 304 st_0 from Σ , with st_0 data user generates a token to be sent to the cloud server and blockchain.
 305 Without the key K_2 , the server cannot compute the current state st from a previous state st_0 ,
 306 therefore it cannot get the current token from a previous, considering that the newly added file f_i
 307 corresponds to the current token, that means the previous tokens cannot match f_i , then forward
 308 security is achieved.

309

310 **Security Analysis**

311 In this section, we analysis the security of our scheme. For the scheme $\Pi = \{\text{KeyGen}, \text{Setup},$
 312 $\text{ClientAuth}, \text{TokenGen}, \text{Search}, \text{Verify}, \text{UpdateToken}, \text{Update}\}$ with the leakage function
 313 $\mathcal{L} = \{\mathcal{L}_{\text{setup}}, \mathcal{L}_{\text{search}}, \mathcal{L}_{\text{update}}\}$, we prove that our scheme is \mathcal{L} -secure against CKA2 by proving that
 314 $\text{Real}_{\mathcal{A}}(\lambda)$ and $\text{Ideal}_{\mathcal{A}, \mathcal{S}}(\lambda)$ are computationally indistinguishable.

315 **Theorem 1.** Our scheme Π is \mathcal{L} -secure against CKA2, if the encryption algorithm is secure
 316 against chosen-plaintext attacks and the pseudo-random function F and H are secure pseudo-
 317 random.

318 **Proof:** We use a probabilistic polynomial time simulator \mathcal{S} to simulate indexes and a series of
 319 tokens. For a PPT adversary \mathcal{A} , we prove theorem 1 by the computational indistinguishability
 320 between $\text{Real}_{\mathcal{A}}(\lambda)$ and $\text{Ideal}_{\mathcal{A}, \mathcal{S}}(\lambda)$. In $\text{Real}_{\mathcal{A}}(\lambda)$, \mathcal{A} gets indexes $(T_B, T$ and $B)$, searches token
 321 $TK_{i,Q}$ and updates token (τ_s, τ_b) by running Setup, TokenGen and UpdateToken; in
 322 $\text{Ideal}_{\mathcal{A}, \mathcal{S}}(\lambda)$, \mathcal{A} gets indexes $(T_B', T'$ and $B')$, searches token $TK_{i,Q}'$ and updates token (τ_s', τ_b')

323 by running $\mathcal{L}_{Setup}, \mathcal{L}_{Search}, \mathcal{L}_{Update}$. We prove that $\text{Real}_{\mathcal{A}}(\lambda)$ and $\text{Ideal}_{\mathcal{A},\mathcal{S}}(\lambda)$ are computational
324 indistinguishable by proving that $(T_B, T, B, TK_{i,Q}, \tau_s, \tau_b)$ and $(T_B', T', B', TK_{i,Q}', \tau_s', \tau_b')$ are
325 indistinguishable.

326 **Simulating index.** \mathcal{S} initializes three empty tables: T', B', T_B' , which are used to store file
327 ciphertexts, verification values and bitmaps, respectively. \mathcal{S} randomly selects a string f_i' of
328 length $|f_i|$, and encrypts it through $c_i' \leftarrow \text{Enc}(K_3, f_i')$, where K_3 is randomly sampled from
329 $\{0,1\}^\lambda$. \mathcal{S} maintains three mappings: H, U and L , H stores $(id_i \| K_3, \ell_i')$, U stores $(H(w_i), u_{w_i}')$,
330 and the mapping L stores $(u_{w_i} \| st_i, t_{w_i}')$. H, U and L are used and updated by the generation of
331 search and update token. \mathcal{S} computes the hash value $hash_i' \leftarrow H(c_i')$, c_i' is stored in $T[l_i']$ and
332 $hash_i'$ is stored in $B[l_i']$. \mathcal{S} selects a string v_{B_j}' of length $|v_{B_j}|$, and stores it in $T_B'[t_{w_i}] \leftarrow v_{B_j}$.

333 T', B' and T_B' are simulated by \mathcal{S} through the leakage \mathcal{L}_{Setup} , the difference between $(T_B',$
334 $T', B')$ and (T_B, T, B) is the generation of (f_i', c_i', v_{B_j}') . In ideal environment, (f_i', c_i', v_{B_j}') are
335 randomly selected, since our encryption algorithm is secure against CKA2, F and H are secure
336 pseudo-random functions, therefore, the probability that the adversary \mathcal{A} can distinguish between
337 the real environment and the ideal environment is negligible.

338 **Simulating search token.** For the keyword w_i to query, \mathcal{S} gets u_{w_i}' from the mapping U
339 through calculating $H(w_i)$, \mathcal{S} checks whether u_{w_i}' is contained in U , if so returns the
340 corresponding entity, otherwise randomly picks a u_{w_i}' in $\{0,1\}^\ell$ and stores $(H(w_i), u_{w_i}')$ in U .
341 Similarly, the experiment gets l_{w_i}' from L by $L[u_{w_i} \| st_i]$, the search token $TK_{i,Q}' = \{l_{w_i}'\}$. Under
342 the assumption that F and H are secure pseudo-random functions, the adversary \mathcal{A} cannot
343 distinguish $TK_{i,Q}$ and $TK_{i,Q}'$.

344 **Simulating update token.** For file f_k to be added, \mathcal{S} first randomly selects a bit string c_k' of
345 length $|f_k|$, and encrypts it through $c_k' \leftarrow \text{Enc}(K_3, f_k')$. \mathcal{S} computes the hash value
346 $hash_k' \leftarrow H(c_k')$, c_k' is stored in $T[l_k']$ and $hash_k'$ is stored in $B[l_k']$, where l_k' is obtained
347 from the mapping H . \mathcal{S} maintains a mapping E , which stores (st_0, st) , if there is no
348 corresponding entity for st , it randomly picks a st in $\{0,1\}^l$, otherwise it returns the corresponding
349 entity. \mathcal{S} gets u_{w_i}' and l_{w_i}' as in search token, selects a string v_{B_j}' of length $|v_{B_j}|$, and stores it in
350 $T_B'[l_{w_j}] \leftarrow v_{B_j}'$. The update token $(\tau_s' = \{(l_k', c_k'), (l_{w_j}', v_{B_j}')\}, \tau_b' = \{(l_k', hash_k'), (l_{w_j}', v_{B_j}')\})$
351 and $(\tau_s = \{(l_k, c_k), (l_{w_j}, v_{B_j})\}, \tau_b = \{(l_k, hash_k), (l_{w_j}, v_{B_j})\})$ are indistinguishable for the adversary
352 \mathcal{A} .

353 In such a way, $(T_B, T, B, TK_{i,Q}, \tau_s, \tau_b)$ and $(T_B', T', B', TK_{i,Q}', \tau_s', \tau_b')$ are indistinguishable
354 for \mathcal{A} , and it means for a PPT adversary \mathcal{A} , the probability of distinguishing between $\text{Real}_{\mathcal{A}}(\lambda)$
355 and $\text{Ideal}_{\mathcal{A},S}(\lambda)$ is negligible, so we have:
356 $|\Pr[\text{Real}_{\mathcal{A}}(\lambda) = 1] - \Pr[\text{Ideal}_{\mathcal{A},S}(\lambda) = 1]| \leq \text{negl}(\lambda)$. Therefore, our scheme satisfies CKA2-security.

357

358 Performance Evaluation

359 In this section, we evaluate the performance of our scheme by constructing a series of experiments,
360 and compare the experimental results with Li et.al (2021) and Guo, Zhang & Jia (2020). Since
361 Guo, Zhang & Jia (2020) does not support multi-keyword search over encrypted data, we compare
362 our scheme with Li et.al (2021) which supports multi-keyword search. Besides, we compare our
363 scheme with Guo, Zhang & Jia (2020) in terms of dynamic operations.

364 We deploy our experiments on a local machine with an Intel Core i7-8550U CPU of 1.80GHz,
365 8GB RAM. We use HMAC-SHA-256 for the pseudo-random functions F , SHA-256 for the hash
366 function H . We use AES as the encryption algorithm to encrypt files. We implement the
367 algorithms in data owner, data user and server using Python and construct the smart contract using
368 Solidity, and the smart contract is tested in with the Ethereum blockchain using a local simulated
369 network TestRPC.

370 For the dataset, we adopt a real-world dataset, Enron email dataset (William, 2015), which
371 contains more than 517 thousand documents. We utilize the Porter Stemmer to extract more than
372 1.67 million keywords and filter that meaningless keywords, such as “of”, “the”. At last, we build
373 an inverted index with those keywords to improve the search efficiency of the experiment.

374

375 Evaluation of Setup

376 In setup phase, data owner encrypts the files, calculates the initial verification values of ciphertexts,
377 generates the bitmap indexes of keywords, stores them in T, B and T_B , respectively.

378 First, we compare the setup time of our scheme with Li et.al (2021) and Guo, Zhang & Jia
379 (2020), the setup time is related to the number of files in the index and the number of keywords
380 included in each file. Figure 3 shows the setup time with different number of keywords in each file
381 while the number of files is fixed at 3137, Fig.4 shows the setup time with different number of
382 files when the number of keywords in each file is fixed at 20. Both figures show that the setup
383 time is affected by the number of keywords in each file and the number of files, and the setup time
384 increases linearly concerning the number of keywords and files.

385 Furthermore, Fig.3 and Fig.4 illustrate that our scheme is more efficient than Li et.al (2021) and
386 Guo, Zhang & Jia (2020) under the same condition in setup time. Since Guo, Zhang & Jia (2020)
387 utilizes the linked list instead of bitmap to build the index, it requires more time than the other
388 schemes. Our scheme takes less time than Li et.al (2021), the reason is that Li et.al (2021) adopts
389 RSA accumulator based on public key encryption to verify multi-keyword search results,

390 in contrast, our scheme utilizes hash functions to verify search results, which reduces the
391 computational overhead greatly.

392

393 **Evaluation of Search**

394 For the performance of our scheme, we compare the search time of our scheme with Li et.al (2021).
395 Moreover, to better evaluate the performance of the scheme in multi-keyword search, we perform
396 two settings in a query: 5 keywords and 10 keywords, respectively. In figures, the suffix of the
397 icon indicates the number of keywords in a query, i.e., Our scheme_5 indicates the search time
398 spent in our scheme during a query which contains 5 keywords, Our scheme_10 indicates the
399 search time spent in our scheme during a query which contains 10 keywords, similarly, Li et.al
400 (2021)_5 and Li et.al (2021)_10 indicates the search time spent in Li et.al (2021) during a query
401 which contains 5 keywords and 10 keywords, respectively.

402 Figure 5 shows the search time with different number of keywords in each file when the number
403 of files is fixed at 3137, and Fig.6 shows the search time with different number of files when the
404 number of keywords in each file is fixed at 20. Both figures show that the search time is affected
405 by the number of keywords in each file and the number of files, and the search time increases sub-
406 linearly with the number of keywords and files.

407 From Fig. 5 and Fig. 6, we can see that the more keywords included in a query, the more time
408 it takes, this is because the more keywords, the search algorithm spends more time to calculate
409 matched files. Another conclusion can be drawn that our scheme is more efficient than Li et.al
410 (2021) in search, the reason is that the same as the setup algorithm, Li et.al (2021) takes more time
411 to calculate the verification values.

412

413 **Evaluation of Verify**

414 Here, we evaluate the performance of our scheme in verification, we verify the results of searching
415 for 5 keywords and 10 keywords respectively, and compares the verification time with Li et.al
416 (2021),the comparison results are shown in Fig.7 and Fig.8. Figure 7 shows the verification time
417 with different number of keywords in each file when the number of files is fixed at 3137, and Fig.8
418 shows the verification time with different number of files when the number of keywords in each
419 file is fixed at 20. From those two figures, we can see that the verification time is affected by the
420 number of keywords in each file and the number of files, the verification time increases with the
421 number of keyword and files.

422 Both figures shows that our scheme gains a higher verification efficiency than Li et.al (2021),
423 the reason is that Li et.al (2021) takes additional time to compute $\mathcal{B}_f = y_i \oplus u_i$, where
424 $u_i = F(K_{f_i} || r_i)$, $K_{f_i} = G(K_3, f_i)$. In addition, the initial verification values in Li et.al (2021) are
425 stored in untrusted server and the verification is performed by the data user, both the server and
426 the user may forge the verification results, while in our scheme, the values are stored in blockchain
427 and the verification is performed by blockchain, cannot be tampered with, hence, our scheme is
428 more fair and secure in verification.

429

430 Evaluation of Update

431 Dynamic update is the important function in SSE, so we evaluate the performance of our scheme
432 in dynamic update by adding a file containing multiple keywords. Figure 9 and Fig.10 show the
433 performance of our scheme, Li et.al (2021) and Guo, Zhang & Jia (2020) in update time, $_5$ and
434 $_10$ indicate that the update document contains 5 keywords and 10 keywords, respectively. We
435 observe that the update time increases with the number of files, since the more files, the longer of
436 the bitmap corresponding to a keyword, then the update algorithm performs more operations when
437 calculating $v_B \leftarrow \mathcal{B}_{w_j} \oplus H(u_{w_j} || st)$. Moreover, the update time is related to the number of
438 keywords contained in the update file, since the more keywords the file contains, the more indexes
439 to update.

440

441 Conclusions

442 In this paper, we present an efficient verifiable multi-keyword search SSE scheme based on
443 blockchain, which accomplishes efficient multi-keyword search and verification. In our scheme,
444 the yardstick of the file is stored on the blockchain, and the verification of the search results is also
445 completed by the blockchain, thus the fairness and reliability of the verification can be ensured. In
446 addition, our solution supports the dynamic update of files and guarantees forward security during
447 the update. Formal security analysis and experimental results show that our scheme is CKA2-
448 security and efficient. Our scheme can be widely used in cloud storage systems such as data
449 outsourcing, cloud-based IoT (Ge et.al, 2021), medical cloud data (Li et.al, 2020),etc., helping to
450 achieve efficient multi-keyword searches, and ensuring the integrity and credibility of search
451 results.

452

453

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