

# Supplementary material

Analysis of affective valence (`affval`) and perceived exertion (`perexe`) outcomes

06 Feb 2023

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## Set up

### Packages

```
suppressPackageStartupMessages(suppressWarnings({  
  
  library("readr")      # read data funcs  
  library("dplyr")       # data manipulation  
  library("tibble")      # improved data frames  
  library("ggplot2")     # plotting  
  library("purrr")       # apply functions over lists/vectors  
  library("forcats")     # handling categorical variables  
  library("tidyverse")    # manipulate data to long/short representations  
  
  library("mice")        # missing value utilities  
  library("car")          # regression utilities  
  
  library("lme4")         # linear mixed effects modelling  
  library("merTools")     # allows prediction intervals using merMod objects  
  library("lmerTest")      # step-wise lmer model selection  
  
  library("knitr")        # pretty printing of tables: kable()  
  library("gtsummary")    # print summary tables of regression mods  
  library("lattice")       # diagnostic plots  
  
}))
```

## Constants

```
### plotting characters
# steep x long: "/"
# steep x short: "))"
# less steep x long: "-"
# less steep x short: "\)"
plchs <-
  c(
    "yes x long" = "|",
    "yes x short" = "/",
    "no x long" = "-",
    "no x short" = "\\"
  )

# plotting colour scheme
col_lohi <-
  c(
    "Lower IAcc" = "darkorange",
    "Higher IAcc" = "purple"
  )
```

## Functions

The below functions make the calculation of Cohen's  $f^2$  effect size statistic on `lme4::lmer()` (`merMod` class objects) possible. These functions are used later after models are fitted.

```
# effect size ( $f^2$ ),  $R^2$  and residual variance functions

get_res_var_lmer <- function(lmer_obj) {
  return(sigma(lmer_obj)^2)
}

get_lmer_r2 <- function(lmer_obj) {

  # residual variance of input model
  v_mod <- get_res_var_lmer(lmer_obj)

  # get formula for null model (intercept and REs only)
  null_form <- formula(lmer_obj, random.only = TRUE)
```

```

# create null model
lmer_obj_null <- update(lmer_obj, null_form)

# res var of null mod
v_null <- get_res_var_lmer(lmer_obj_null)

r2 <- (v_null - v_mod) / v_null

attr(r2, "v_null") <- v_null
attr(r2, "v_mod") <- v_mod

return(r2)
}

rm_terms_lmer <- function(lmer_obj, terms) {

  update_form <- as.formula(paste0("~ . -", paste(terms, collapse = " - ")))
  print(update_form)

  lmer_obj_less_term <- update(lmer_obj, update_form)

  return(lmer_obj_less_term)
}

eff_size_f2 <- function(lmer_obj, terms) {

  r2_full <- get_lmer_r2(lmer_obj)[1]
  r2_less_term <- get_lmer_r2(rm_terms_lmer(lmer_obj, terms))[1]

  f2 <- (r2_full - r2_less_term) / (1 - r2_full)

  return(f2)
}

```

Convenience function for tidy printing of data.

```

# function that replaces repeated values in a vector with empty strings
# as the verbose redundancy is too busy in some cases

```

```
rm_rpts <- function(x) {  
  x <- as.character(x)  
  nx <- length(x)  
  rm_ii <- rep(FALSE, nx)  
  for (i in 2:nx) {  
    if (x[i - 1] == x[i])  
      rm_ii[i] <- TRUE  
  }  
  x[rm_ii] <- ""  
  return(x)  
}
```

# Data

## Import

```
dat_col_spec <-  
  cols(  
    partic = col_integer(),  
    affval = col_integer(),  
    perexe = col_integer(),  
    int_sens = col_double(),  
    block = col_integer(),  
    cond = col_character(),  
    steep = col_character(),  
    dist = col_character()  
)  
  
# read in dataset  
hill_dat <- read_csv("dat/seefei-hill-dat.csv", col_types = dat_col_spec)  
  
# have a peak  
hill_dat
```

## Wrangling

```
# make factor variables and default levels  
hill_dat <-  
  hill_dat %>%  
  mutate(  
    cond = factor(cond),  
    cond = relevel(cond, ref = "flat"),  
    steep = factor(steep),  
    steep = relevel(steep, ref = "no"),  
    dist = factor(dist),  
    dist = relevel(dist, ref = "short"),  
    block = factor(block)  
)  
  
# NAs only present in outcome vars  
# md.pattern(hill_dat, rotate.names = TRUE)
```

```

### centring the int_sens variable for easier interpretation of model intercept terms
# NOTE: want average of average participant values
isc <-
  hill_dat %>%
  group_by(partic) %>%
  summarise(avg_int_sens = mean(int_sens))

# This is the mean ISC over participants
mean_isc <- isc %>% pull(avg_int_sens) %>% mean(.)
sd_isc <- isc %>% pull(avg_int_sens) %>% sd(.)

# now modify the ISC values in the data
hill_dat <-
  hill_dat %>%
  mutate(int_sens = int_sens - mean_isc)

```

## Model predictions dataset

This step creates a dataset for predictions from the models used later on.

```

# create a minimal prediction dataset
pred_dat <-
  hill_dat %>%
  distinct(cond, block) %>%
  # NB: this is the mean ISC as we centred this data previously
  mutate(int_sens = 0, partic = 1L)

pred_dat_isc_plus_sd <-
  pred_dat %>%
  mutate(int_sens = int_sens + sd_isc)

pred_dat_isc_less_sd <-
  pred_dat %>%
  mutate(int_sens = int_sens - sd_isc)

pred_dat <-
  bind_rows(pred_dat_isc_less_sd, pred_dat, pred_dat_isc_plus_sd) %>%
  as.data.frame(.)

```

# Modelling

**Outcome:** affval

**Stepwise selection and final model**

```
hill_dat_affmod <- subset(hill_dat, !is.na(affval))

# largest potential model
m1 <-
  lmer(
    affval ~
      int_sens * (cond + steep + dist + block) +
      (1 | partic),
    data = hill_dat_affmod,
    REML = FALSE
  )
# summary(m1)

# elimination of non-significant effects
# partly thanks to code found at::
# https://www.rdocumentation.org/packages/lmerTest/versions/2.0-36/topics/step
s1 <- step(m1) # consider optional arguments: test = c("none", "Rao", "LRT", "Chisq", "F")

# look at the model reduction
print(s1)
```

Backward reduced random-effect table:

	Eliminated	npar	logLik	AIC	LRT	Df	Pr(>Chisq)				
<none>		18	-1307.5	2651.0							
(1   partic)		0	17	-1820.1	3674.2	1025.3	1 < 2.2e-16 ***				
---											
Signif. codes:	0	'***'	0.001	'**'	0.01	'*'	0.05	'. '	0.1	' '	1

Backward reduced fixed-effect table:

Degrees of freedom method: Satterthwaite

	Eliminated	Sum Sq	Mean Sq	NumDF	DenDF	F value	Pr(>F)
int_sens:cond	1	0.4492	0.2246	2	933.00	0.2722	0.7618
int_sens:dist	2	0.6639	0.6639	1	933.01	0.8041	0.3701

```

dist              3  0.4016  0.4016      1 933.00  0.4859  0.4859
int_sens:steep   4  0.7588  0.7588      1 933.00  0.9178  0.3383
steep             5  0.2503  0.2503      1 933.00  0.3025  0.5825
cond              0 17.0005  8.5002      2 933.00  10.2672 3.885e-05 ***
int_sens:block   0 25.9216  8.6405      3 933.01  10.4367 9.309e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Model found:

```
affval ~ int_sens + cond + block + (1 | partic) + int_sens:block
```

```
# plot of post-hoc analysis of the final model
# plot(s1)
```

```
# use REML for final fit... see the following links
# https://stats.stackexchange.com/questions/41123/reml-vs-ml-stepaic
# https://stats.stackexchange.com/questions/116770/reml-or-ml-to-compare-two-mixed-effects
# https://stats.stackexchange.com/questions/414551/forward-selection-with-mixed-model-using
m1_final <-
  lmer(
    affval ~ int_sens + cond + block + int_sens:block +
      (1 | partic),
    data = hill_dat_affmod,
    REML = TRUE
  )
summary(m1_final)
```

```
Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula: affval ~ int_sens + cond + block + int_sens:block + (1 | partic)
Data: hill_dat_affmod
```

REML criterion at convergence: 2628.4

Scaled residuals:

Min	1Q	Median	3Q	Max
-4.8486	-0.4947	0.0079	0.4971	4.3849

Random effects:

Groups	Name	Variance	Std.Dev.
--------	------	----------	----------

```

partic  (Intercept) 2.0548   1.4334
Residual           0.8351   0.9138
Number of obs: 953, groups: partic, 20

Fixed effects:
Estimate Std. Error      df t value Pr(>|t|)
(Intercept)    9.18774   0.32866 19.56035 27.955 < 2e-16 ***
int_sens      -4.09769   3.01158 18.95131 -1.361 0.189589
conddownhill  -0.21401   0.07242 924.99970 -2.955 0.003202 **
conduphill     0.10722   0.07260 925.00232  1.477 0.140037
block2        -0.30735   0.08379 925.00216 -3.668 0.000258 ***
block3        -0.52714   0.08370 925.00199 -6.298 4.65e-10 ***
block4        -0.80794   0.08397 925.00476 -9.622 < 2e-16 ***
int_sens:block2 1.16392   0.77901 925.00736  1.494 0.135488
int_sens:block3 3.17178   0.77612 925.00438  4.087 4.75e-05 ***
int_sens:block4 3.83155   0.78079 925.01026  4.907 1.09e-06 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Correlation of Fixed Effects:
              (Intr) int_sn cnddwn cndphl block2 block3 block4 int_:_2 int_:_3
int_sens       0.001
conddownhill -0.110  0.000
conduphill    -0.110  0.000  0.500
block2         -0.128 -0.002  0.000  0.002
block3         -0.128 -0.002  0.000  0.000  0.503
block4         -0.128 -0.002 -0.002  0.002  0.501  0.502
int_sns:bl2   -0.002 -0.130  0.000 -0.004  0.006  0.010  0.010
int_sns:bl3   -0.002 -0.131  0.000 -0.001  0.010  0.010  0.010  0.505
int_sns:bl4   -0.003 -0.130  0.002  0.005  0.010  0.010  0.012  0.502  0.504

# term significance -- Type III Wald chi-square tests
car::Anova(m1_final, type = "III")

```

#### Analysis of Deviance Table (Type III Wald chisquare tests)

```

Response: affval
          Chisq Df Pr(>Chisq)
(Intercept) 781.4956  1 < 2.2e-16 ***
int_sens     1.8514  1     0.1736
cond         20.3573  2  3.797e-05 ***

```

```

block          99.5601  3 < 2.2e-16 ***
int_sens:block 31.0369  3 8.350e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

# prettier printing of regression model
m1_final %>%
 tbl_regression(
  estimate_fun = function(x) sprintf("%2.2f", x),
  pvalue_fun = function(x) sprintf("%1.8f", x)
) %>%
  add_global_p(keep = TRUE) %>%
  as_gt()

```

Characteristic	Beta	95% CI <sup>1</sup>	p-value
int_sens	-4.10	-10.40, 2.21	0.17362526
cond			0.00003797
flat	—	—	
downhill	-0.21	-0.36, -0.07	0.00320211
uphill	0.11	-0.04, 0.25	0.14003749
block			0.00000000
1	—	—	
2	-0.31	-0.47, -0.14	0.00025820
3	-0.53	-0.69, -0.36	0.00000000
4	-0.81	-0.97, -0.64	0.00000000
int_sens * block			0.00000083
int_sens * 2	1.16	-0.36, 2.69	0.13548840
int_sens * 3	3.17	1.65, 4.69	0.00004755
int_sens * 4	3.83	2.30, 5.36	0.00000109

<sup>1</sup>CI = Confidence Interval

## Effect size calculations

```

### testing and extracting model elements for f^2 calc
# terms(formula(m1_final, fixed.only = TRUE))
# summary(m1_final)
# summary(rm_terms_lmer(m1_final, "cond"))
# summary(rm_terms_lmer(m1_final, c("int_sens", "int_sens:block")))

```

```

### test functions
# get_lmer_r2(m1_final)
# get_lmer_r2(rm_terms_lmer(m1_final, "cond"))
### need to consider higher level terms with main effects
# get_lmer_r2(rm_terms_lmer(m1_final, c("int_sens", "int_sens:block")))

# cond eff size
eff_size_f2(m1_final, "cond")

~. - cond
<environment: 0x000000003006cf70>

[1] 0.01979127

(get_lmer_r2(m1_final) -
  get_lmer_r2(rm_terms_lmer(m1_final, c("cond")))) /
(1 - get_lmer_r2(m1_final)) # manual check

~. - cond
<environment: 0x0000000026b6c268>

[1] 0.01979127
attr(,"v_null")
[1] 0.9641614
attr(,"v_mod")
[1] 0.8350603

# int_sens eff size
eff_size_f2(m1_final, c("int_sens", "int_sens:block"))

~. - int_sens - int_sens:block
<environment: 0x000000002f9d8770>

[1] 0.03016223

```

```

(get_lmer_r2(m1_final) -
  get_lmer_r2(rm_terms_lmer(m1_final, c("int_sens", "int_sens:block")))) /
(1 - get_lmer_r2(m1_final)) # manual check

~. - int_sens - int_sens:block
<environment: 0x000000002587e0a8>

[1] 0.03016223
attr(,"v_null")
[1] 0.9641614
attr(,"v_mod")
[1] 0.8350603

# interaction only eff size
eff_size_f2(m1_final, "int_sens:block")

~. - int_sens:block
<environment: 0x000000002fc19e20>

[1] 0.03016245

(get_lmer_r2(m1_final) -
  get_lmer_r2(rm_terms_lmer(m1_final, "int_sens:block")))/
(1 - get_lmer_r2(m1_final)) # manual check

~. - int_sens:block
<environment: 0x0000000025b5be78>

[1] 0.03016245
attr(,"v_null")
[1] 0.9641614
attr(,"v_mod")
[1] 0.8350603

```

### Model predicted affval

```

# ?predict.merMod
# ?predict

#### usage
# predict(
#   object, newdata = NULL, newparams = NULL,
#   re.form = ~0, # or NULL for no REs
#   random.only = FALSE, terms = NULL,
#   type = c("link", "response"), allow.new.levels = FALSE,
#   na.action = na.pass, ...
# )

# test the above centring claim
# hist(hill_dat$int_sens_cont)

pred_est <-
  predict(
    m1_final,
    newdata = pred_dat,
    re.form = ~0
  )

# see:
# https://cran.r-project.org/web/packages/merTools/vignettes/Using_predictInterval.html
# ?merTools::predictInterval

pred_ci_est <-
  merTools:::predictInterval(
    merMod = m1_final,
    newdata = pred_dat,
    which = c("full", "fixed", "random", "all")[4],
    level = 0.95,
    n.sims = 1000,
    stat = "median",
    type = "linear.prediction",
    include.resid.var = TRUE, # TRUE for including
    # fix.intercept.variance = TRUE
    seed = 1234567890
  ) %>%

```

```

dplyr::filter(effect == "fixed") %>%
arrange(obs)

pred_dat_aff <-
bind_cols(pred_dat, tibble(fit_analytic = pred_est), pred_ci_est) %>%
as_tibble()

# cat("#### Min and max difference between analytic fit and bootstrap median is:\n")
# with(pred_dat_aff, min(fit_analytic - fit))
# with(pred_dat_aff, max(fit_analytic - fit))

# pred_dat_aff %>%
#   dplyr::select(cond, block, int_sens, fit, lwr, upr) %>%
#   kable(., digits = 2)

pred_dat_aff <-
pred_dat_aff %>%
mutate(
  ISC_value =
  ifelse(
    int_sens < (0 - sd_isc/2),
    "Lower IAcc", # mean(IAcc) - sd(IAcc)
    ifelse(
      int_sens > (0 + sd_isc/2),
      "Higher IAcc", # mean(IAcc) + sd(IAcc),
      "Mean IAcc" # mean(IAcc)
    )
  ),
  ISC_value = factor(ISC_value),
  ISC_value = relevel(ISC_value, ref = "Lower IAcc"),
  cond = relevel(cond, ref = "downhill")
)

# change likert scale data recorded as [1, 12] to [-5, 5]
likert_adj <- -6

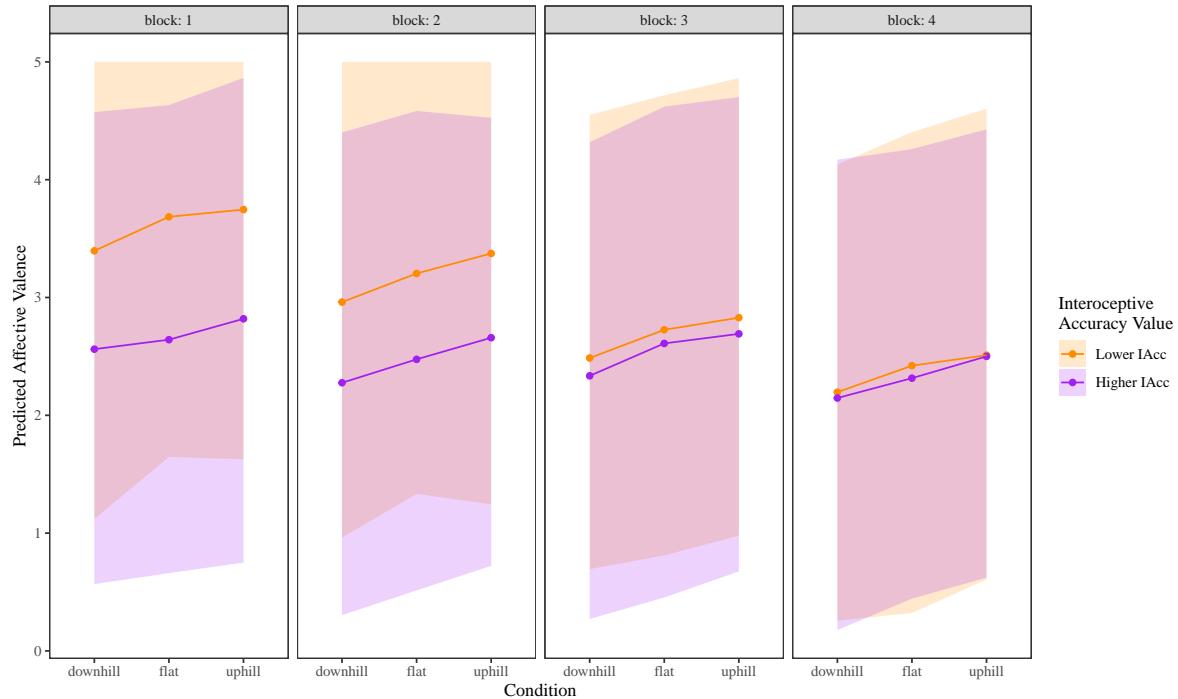
pred_dat_aff %>%
dplyr::filter(ISC_value != "Mean IAcc") %>%
mutate(
  trunc_up = if_else(upr > 11, 11L, as.integer(NA)),

```

```

upr = if_else(!is.na(trunc_up), 11, upr),
fit = fit + likert_adj,
lwr = lwr + likert_adj,
upr = upr + likert_adj
) %>%
ggplot(data = ., aes(x= factor(cond), y = fit, col = ISC_value, group = ISC_value)) +
geom_ribbon(aes(ymax = upr, ymin = lwr, fill = ISC_value), alpha = 0.2, colour = NA) +
geom_point() +
geom_line() +
facet_wrap(~ block, ncol = 4, labeller = label_both) +
theme_bw() +
theme(text = element_text(family = "serif"), panel.grid = element_blank()) +
scale_color_manual(values = col_lohi) +
scale_fill_manual(values = col_lohi) +
labs(
  y = "Predicted Affective Valence",
  x = "Condition",
  col = "Interoceptive\\nAccuracy Value",
  fill = "Interoceptive\\nAccuracy Value"
)

```



## Outcome: perexe

### Stepwise selection and final model

```
hill_dat_permod <- subset(hill_dat, !is.na(perexe))

# largest potential model
m2 <-
  lmer(
    perexe ~
      int_sens * (cond + steep + dist + block) +
      (1 | partic),
    data = hill_dat_permod,
    REML = FALSE
  )
# summary(m2)

# elimination of non-significant effects
s2 <- step(m2)

# look at the model reduction
print(s2)
```

Backward reduced random-effect table:

	Eliminated	npar	logLik	AIC	LRT	Df	Pr(>Chisq)
<none>		18	-1610.5	3257.0			
(1   partic)		0	17	-2048.8	4131.6	876.65	1 < 2.2e-16 ***
---							
Signif. codes:	0	'***'	0.001	'**'	0.01	'*'	0.05 '. '
							0.1 ' ' 1

Backward reduced fixed-effect table:

Degrees of freedom method: Satterthwaite

	Eliminated	Sum Sq	Mean Sq	NumDF	DenDF	F value	Pr(>F)
int_sens:dist	1	0.058	0.0580	1	938	0.0376	0.8462
dist	2	0.012	0.0125	1	938	0.0081	0.9282
int_sens:steep	3	0.265	0.2645	1	938	0.1718	0.6786
steep	4	0.325	0.3250	1	938	0.2110	0.6461
int_sens:cond	0	47.519	23.7597	2	938	15.4232	2.568e-07 ***
int_sens:block	0	54.450	18.1501	3	938	11.7818	1.400e-07 ***

```

---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Model found:
perexe ~ int_sens + cond + block + (1 | partic) + int_sens:cond + int_sens:block

# use REML for final fit
m2_final <-
lmer(
  perexe ~ int_sens + cond + block +
  int_sens:cond + int_sens:block +
  (1 | partic),
  data = hill_dat_permod,
  REML = TRUE
)
summary(m2_final)

Linear mixed model fit by REML. t-tests use Satterthwaite's method [
lmerModLmerTest]
Formula: perexe ~ int_sens + cond + block + int_sens:cond + int_sens:block +
(1 | partic)
Data: hill_dat_permod

REML criterion at convergence: 3223.2

Scaled residuals:
    Min      1Q  Median      3Q     Max
-4.7274 -0.6103 -0.0234  0.6248  2.8202

Random effects:
Groups   Name        Variance Std.Dev.
partic   (Intercept) 2.989    1.729
Residual           1.557    1.248
Number of obs: 958, groups: partic, 20

Fixed effects:
            Estimate Std. Error       df t value Pr(>|t|)
(Intercept) 10.44367  0.39904 19.98855 26.172 < 2e-16 ***
int_sens    -1.82776  3.68550 19.98716 -0.496  0.6254
conddownhill  0.25032  0.09873 927.99928  2.535  0.0114 *
conduphill   -0.19832  0.09873 927.99933 -2.009  0.0449 *
```

```

block2          0.84316   0.11416  928.00025   7.386 3.37e-13 ***
block3          1.38066   0.11416  928.00025  12.094 < 2e-16 ***
block4          1.71399   0.11416  928.00025  15.014 < 2e-16 ***
int_sens:conddownhill 4.29035   0.91235  927.99966   4.703 2.96e-06 ***
int_sens:conduphill    4.42798   0.91115  927.99868   4.860 1.38e-06 ***
int_sens:block2       -2.80558   1.05396  927.99999  -2.662  0.0079 **
int_sens:block3       -4.27832   1.05396  927.99999  -4.059 5.34e-05 ***
int_sens:block4       -6.00929   1.05396  927.99999  -5.702 1.59e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Correlation of Fixed Effects:

	(Intr)	int_sn	cnddwn	cndphl	block2	block3	block4	int_sns:cndd
int_sens	0.000							
conddownhill	-0.123	0.001						
conduphill	-0.123	0.000	0.499					
block2	-0.143	-0.001	-0.002	-0.002				
block3	-0.143	-0.001	-0.002	-0.002	0.502			
block4	-0.143	-0.001	-0.002	-0.002	0.502	0.502		
int_sns:cndd	0.001	-0.123	0.002	0.000	-0.002	-0.002	-0.002	
int_sns:cndp	0.000	-0.124	0.000	0.000	0.000	0.000	0.000	0.499
int_sns:bl2	-0.001	-0.143	-0.002	0.000	0.003	0.003	0.003	-0.003
int_sns:bl3	-0.001	-0.143	-0.002	0.000	0.003	0.003	0.003	-0.003
int_sns:bl4	-0.001	-0.143	-0.002	0.000	0.003	0.003	0.003	-0.003
					int_sns:cndp	int:_:2	int:_:3	
int_sens								
conddownhill								
conduphill								
block2								
block3								
block4								
int_sns:cndd								
int_sns:cndp								
int_sns:bl2	0.000							
int_sns:bl3	0.000		0.502					
int_sns:bl4	0.000		0.502	0.502				

```

# term significance
car::Anova(m2_final, type = "III")

```

Analysis of Deviance Table (Type III Wald chisquare tests)

```

Response: perexe
            Chisq Df Pr(>Chisq)
(Intercept) 684.9663 1 < 2.2e-16 ***
int_sens     0.2459  1     0.6199
cond         20.7084 2  3.186e-05 ***
block        257.4023 3 < 2.2e-16 ***
int_sens:cond 30.5175 2  2.362e-07 ***
int_sens:block 34.9684 3  1.237e-07 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

# prettier printing of regression model
m2_final %>%
 tbl_regression(
  estimate_fun = function(x) sprintf("%2.2f", x),
  pvalue_fun = function(x) sprintf("%1.8f", x)
) %>%
add_global_p(keep = TRUE) %>%
as_gt()

```

Characteristic	Beta	95% CI <sup>1</sup>	p-value
int_sens	-1.83	-9.52, 5.86	0.61994148
cond			0.00003186
flat	—	—	
downhill	0.25	0.06, 0.44	0.01139471
uphill	-0.20	-0.39, -0.00	0.04485907
block			0.00000000
1	—	—	
2	0.84	0.62, 1.07	0.00000000
3	1.38	1.16, 1.60	0.00000000
4	1.71	1.49, 1.94	0.00000000
int_sens * cond			0.00000024
int_sens * downhill	4.29	2.50, 6.08	0.00000296
int_sens * uphill	4.43	2.64, 6.22	0.00000138
int_sens * block			0.00000012
int_sens * 2	-2.81	-4.87, -0.74	0.00790347
int_sens * 3	-4.28	-6.35, -2.21	0.00005337
int_sens * 4	-6.01	-8.08, -3.94	0.00000002

<sup>1</sup>CI = Confidence Interval

## Effect size calculations

```
### testing and extracting model elements for f^2 calc
# terms(formula(m2_final, fixed.only = TRUE))
# summary(m2_final)
# summary(rm_terms_lmer(m2_final, c("int_sens", "int_sens:block")))

# interaction int_sens:block only eff size
eff_size_f2(m2_final, "int_sens:cond")

~. - int_sens:cond
<environment: 0x000000002fae1930>

[1] 0.03066341

(get_lmer_r2(m2_final) -
  get_lmer_r2(rm_terms_lmer(m2_final, "int_sens:cond"))) /
(1 - get_lmer_r2(m2_final)) # manual check

~. - int_sens:cond
<environment: 0x00000000195754b8>

[1] 0.03066341
attr(,"v_null")
[1] 2.112033
attr(,"v_mod")
[1] 1.557121

# interaction int_sens:block only eff size
eff_size_f2(m2_final, "int_sens:block")

~. - int_sens:block
<environment: 0x000000002bcb0c30>

[1] 0.03433652
```

```

(get_lmer_r2(m2_final) -
  get_lmer_r2(rm_terms_lmer(m2_final, "int_sens:block")) /
(1 - get_lmer_r2(m2_final)) # manual check

~. - int_sens:block
<environment: 0x000000002e6003b8>

[1] 0.03433652
attr(,"v_null")
[1] 2.112033
attr(,"v_mod")
[1] 1.557121

```

### Model predicted perexe

```

# test the above centring claim
# hist(hill_dat$int_sens_cont)

pred_est <-
  predict(
    m2_final,
    newdata = pred_dat,
    re.form = ~0
  )

pred_ci_est <-
  merTools::predictInterval(
    merMod = m2_final,
    newdata = pred_dat,
    which = c("full", "fixed", "random", "all")[4],
    level = 0.95,
    n.sims = 1000,
    stat = "median",
    type = "linear.prediction",
    include.resid.var = TRUE, # TRUE for including
    # fix.intercept.variance = TRUE
    seed = 1234567890
  ) %>%

```

```

dplyr::filter(effect == "fixed") %>%
arrange(obs)

pred_dat_per <-
bind_cols(pred_dat, tibble(fit_analytic = pred_est), pred_ci_est) %>%
as_tibble()

# cat("#### Min and max difference between analytic fit and bootstrap median is:\n")
# with(pred_dat_per, min(fit_analytic - fit))
# with(pred_dat_per, max(fit_analytic - fit))

# pred_dat_per %>%
#   dplyr::select(cond, block, int_sens, fit, lwr, upr) %>%
#   kable(., digits = 2)

pred_dat_per <-
pred_dat_per %>%
mutate(
  ISC_value =
  ifelse(
    int_sens < (0 - sd_isc/2),
    "Lower IAcc", # mean(IAcc) - sd(IAcc)
    ifelse(
      int_sens > (0 + sd_isc/2),
      "Higher IAcc", # mean(IAcc) + sd(IAcc),
      "Mean IAcc" # mean(IAcc)
    )
  ),
  ISC_value = factor(ISC_value),
  ISC_value = relevel(ISC_value, ref = "Lower IAcc"),
  cond = relevel(cond, ref = "downhill")
)

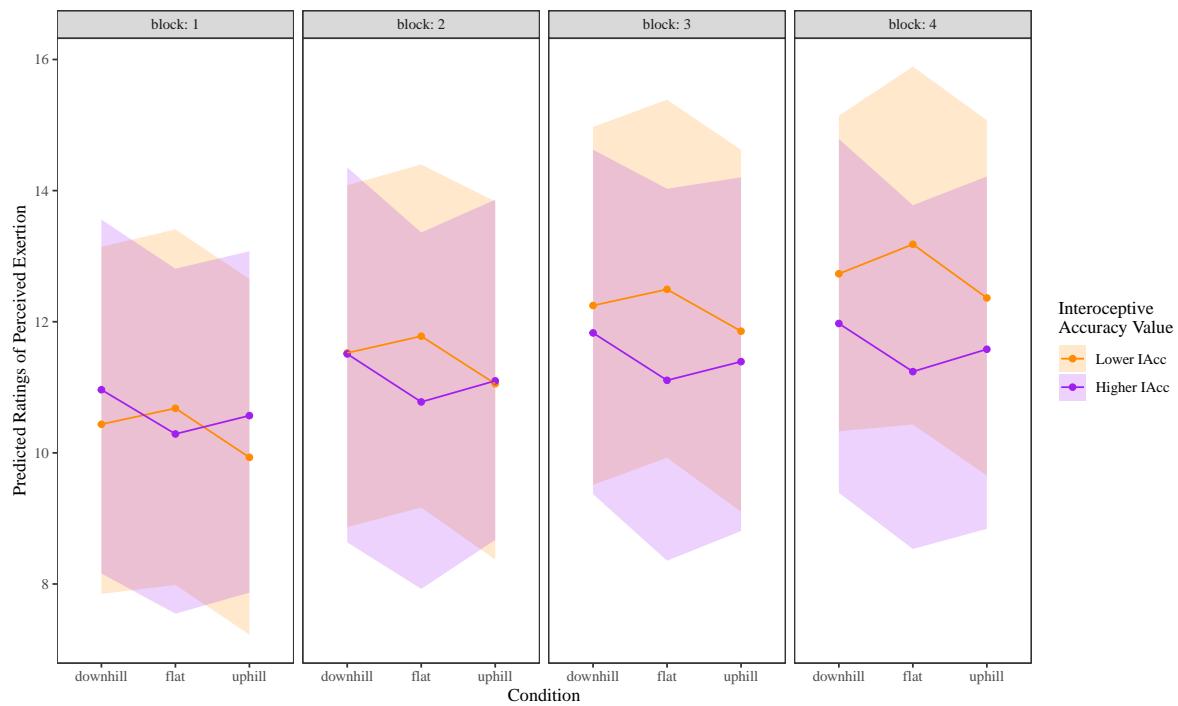
pred_dat_per %>%
  dplyr::filter(ISC_value != "Mean IAcc") %>%
  ggplot(data = ., aes(x= factor(cond), y = fit, col = ISC_value, group = ISC_value)) +
  geom_ribbon(aes(ymax = upr, ymin = lwr, fill = ISC_value), alpha = 0.2, colour = NA) +
  geom_point() +
  geom_line() +
  facet_wrap(~ block, ncol = 4, labeller = label_both) +

```

```

theme_bw() +
theme(text = element_text(family = "serif"), panel.grid = element_blank()) +
scale_color_manual(values = col_lohi) +
scale_fill_manual(values = col_lohi) +
labs(
  y = "Predicted Ratings of Perceived Exertion",
  x = "Condition",
  col = "Interoceptive\\nAccuracy Value",
  fill = "Interoceptive\\nAccuracy Value"
)

```



## R session information

```
# for reproducibility
sessionInfo()

R version 4.1.3 (2022-03-10)
Platform: x86_64-w64-mingw32/x64 (64-bit)
Running under: Windows 10 x64 (build 19044)

Matrix products: default

locale:
[1] LC_COLLATE=English_Australia.1252  LC_CTYPE=English_Australia.1252
[3] LC_MONETARY=English_Australia.1252 LC_NUMERIC=C
[5] LC_TIME=English_Australia.1252

attached base packages:
[1] stats      graphics   grDevices utils      datasets   methods    base

other attached packages:
[1] lattice_0.20-45 gtsummary_1.6.1 knitr_1.37      lmerTest_3.1-3
[5] merTools_0.5.2  arm_1.13-1     MASS_7.3-55      lme4_1.1-28
[9] Matrix_1.5-3   car_3.0-12    carData_3.0-5   mice_3.15.0
[13] tidyverse_1.2.0forcats_0.5.1 purrr_0.3.4    ggplot2_3.4.0
[17] tibble_3.1.8  dplyr_1.0.10  readr_2.1.2

loaded via a namespace (and not attached):
[1] bit64_4.0.5          vroom_1.5.7        jsonlite_1.8.0
[4] splines_4.1.3         foreach_1.5.2       shiny_1.7.4
[7] assertthat_0.2.1      broom.mixed_0.2.9.4 yaml_2.3.5
[10] globals_0.16.2        numDeriv_2016.8-1.1 pillar_1.8.1
[13] backports_1.4.1       glue_1.6.2         digest_0.6.29
[16] promises_1.2.0.1      minqa_1.2.4       colorspace_2.1-0
[19] htmltools_0.5.4       httpuv_1.6.8       pkgconfig_2.0.3
[22] labelled_2.9.1       broom_1.0.1        listenv_0.9.0
[25] haven_2.5.0          xtable_1.8-4       mvtnorm_1.1-3
[28] scales_1.2.1          later_1.3.0       tzdb_0.2.0
[31] farver_2.1.1          generics_0.1.3     ellipsis_0.3.2
[34] withr_2.5.0           furrr_0.3.0        cli_3.6.0
[37] crayon_1.5.2          magrittr_2.0.2     mime_0.12
[40] evaluate_0.20         future_1.30.0     fansi_1.0.4
```

```
[43] parallelly_1.34.0      broom.helpers_1.8.0 nlme_3.1-155
[46] tools_4.1.3           hms_1.1.1          lifecycle_1.0.3
[49] stringr_1.5.0         munsell_0.5.0   compiler_4.1.3
[52] rlang_1.0.6           blme_1.0-5       grid_4.1.3
[55] nloptr_2.0.3          gt_0.7.0          iterators_1.0.14
[58] rstudioapi_0.13       labeling_0.4.2  rmarkdown_2.20
[61] boot_1.3-28           gtable_0.3.1    codetools_0.2-18
[64] abind_1.4-5           DBI_1.1.2        R6_2.5.1
[67] bit_4.0.4              fastmap_1.1.0  utf8_1.2.2
[70] commonmark_1.8.1      stringi_1.7.12 parallel_4.1.3
[73] Rcpp_1.0.10            vctrs_0.5.2    tidyselect_1.2.0
[76] xfun_0.36              coda_0.19-4
```